

RESEARCH DISCUSSION PAPER

A Structural Model of Australia as a Small Open Economy

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### Abstract

This paper sets up and estimates a structural model of Australia as a small open economy using Bayesian techniques. Unlike other recent studies, the paper shows that a small micro-founded model can capture the open economy dimensions quite well. Specifically, the model attributes a substantial fraction of the volatility of domestic output and inflation to foreign disturbances and matches the evidence from reduced-form studies. In addition, the model relies much less than other estimated models on a persistent shock to the risk premium to explain changes in the nominal exchange rate. The paper also investigates the effects of various exogenous shocks on the Australian economy.

> JEL Classification Numbers: E30, F41 Keywords: small open economy, Australia, Bayesian methods

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# A STRUCTURAL MODEL OF AUSTRALIA AS A SMALL OPEN ECONOMY

### **Kristoffer Nimark**

### 1. Introduction

This paper presents and estimates a small structural model of the Australian economy with the aim of providing both a theoretically rigorous framework as well as rich enough dynamics to make the model empirically plausible. The economics of the model are simple. Households choose how much to consume and how much labour to supply. Firms choose prices and then produce enough goods to meet demand. A fraction of the domestically produced goods are exported and a fraction of the domestically consumed goods are imported, with the size of the fractions determined by the relative price of goods produced at home and abroad. This is the minimal structure needed to capture the open economy dimension of the Australian economy, and it is similar to that used in many other studies, for example Lubik and Schorfheide (forthcoming), Galí and Monacelli (2005) and Justiniano and Preston (2005). In addition to this basic structure, the model is amended to account for the importance of the commodities sector for Australian exports by adding exogenous export demand and income shocks.

Estimated models derived from micro foundations have become popular tools at central banks around the world. One often-cited reason for this is that structural models can be used to produce counterfactual scenarios, as well as to make predictions about how macroeconomic outcomes would change if alternative policies were implemented. Nessén (2006) provides a useful perspective on how small structural models can be used in the policy process. She argues that a model is not a tool that provides answers to questions, but rather a framework of principles in which a structured and transparent analysis can be conducted.

For any model to be a useful analytical tool, however, one first needs to establish whether it provides a reasonable description of the data. In a series of papers, Smets and Wouters (2003, 2004) show that medium-scale models can fit the dynamics of a large (closed) economy well. Some recent papers have asked whether structural open economy models can provide a similarly good fit.<sup>1</sup> Particularly, Justiniano and Preston (2005) question whether these models can account for the influence of foreign shocks on the domestic economy. This paper shows that the influence of foreign shocks can indeed be captured by the dynamics of a small structural model. In addition to matching the magnitude of the influence of foreign shocks found by reduced-form methods, the model presented here can also explain a larger fraction of the nominal exchange rate variability endogenously than previous studies.<sup>2</sup>

The model is estimated using Bayesian methods that exploit information from outside the data sample to generate posterior estimates of the structural parameters. The number of time series used is larger than in most other studies to ensure that the data span the open economy dimension of the model. The magnitude of measurement errors in some of the observable time series used is also estimated. This not only allows for errors in the data introduced through the data collection process, but also recognises the fact that some of the theoretical variables of the model do not have clear-cut observable counterparts. This approach also allows something to be said about how well these time series fit the cross-equation and dynamic implications of the model.

# 2. A Small-scale Model of Australia

The structural model is in most respects a standard New Keynesian small open economy model. But the model has a number of adjustments to account for some features of the Australian economy that are peculiar compared to many other developed countries. In particular, while international trade for most developed countries appears be driven by benefits that come from specialisation, Australia's external trade appears to be driven more by classical comparative advantage, with exports dominated by primary products, while more than half of imports are manufactured goods.<sup>3</sup> In the standard model, the demand for a country's exports are determined by the level of world output and the domestic relative cost of

<sup>&</sup>lt;sup>1</sup> See, for instance, Justiniano and Preston (2005) and Fukac, Pagan and Pavlov (2006).

<sup>&</sup>lt;sup>2</sup> See Lubik and Schorfheide (2005), Lindé, Nessén and Söderström (2004) and Justiniano and Preston (2005).

<sup>&</sup>lt;sup>3</sup> See Department of Foreign Affairs and Trade (2005).

production. Australia can be considered to be a price taker in many of its export markets and has little influence over the price of its exports. Exogenous shocks are therefore added to both the volume of export demand as well as the price that exporters receive for their goods.

Australia is also considered a *small* economy in the model in the sense that macroeconomic outcomes and policy in Australia are assumed to have no discernable impact on world output, inflation and interest rates. These foreign variables are thus modelled as being exogenous to Australia.

### 2.1 Household Preferences

A continuum of households populate the economy, consume goods and supply labour to firms. Consider a representative household indexed by  $i \in (0,1)$  that wishes to maximise the discounted sum of its expected utility

$$E_t \left\{ \sum_{s=0}^{\infty} \beta^s U\left( C_{t+s}(i), N_{t+s}(i) \right) \right\}$$
(1)

where  $\beta \in (0,1)$  is the household's subjective discount factor. The period utility function in consumption  $C_t$  and labour  $N_t$  is given by

$$U(C_t(i), N_t(i)) = \frac{\left(C_t(i)H_t^{-\eta}\right)^{1-\gamma}}{(1-\gamma)} - \frac{N_t(i)^{1+\varphi}}{1+\varphi}$$
(2)

and reflects the fact that households like to consume but dislike work. The variable  $H_t$ 

$$H_t = \int C_{t-1}(i) \, di \tag{3}$$

is a reference level of consumption capturing the notion that households not only care about their own consumption, but also care about the lagged consumption of others. This feature – often referred to as 'external habits' or a preference for 'catching up with the Joneses' – helps to explain the inertia of aggregate output, since past levels of aggregate consumption are positively related to the marginal utility of current consumption under this set-up.

### 2.2 The Consumption Bundle

Households' preferences are specified over a continuum of differentiated goods that enter the households' utility function with decreasing marginal weight. Households thus prefer to consume a mixture of differentiated goods rather than consuming just one variety. The consumption bundle  $C_t$  is a constant elasticity of substitution (CES) aggregated index of domestically produced and imported sub-bundles  $C_t^d$  and  $C_t^m$ 

$$C_t \equiv \left[ (1-\alpha)^{\frac{1}{\delta}} C_t^{d\frac{\delta-1}{\delta}} + \alpha^{\frac{1}{\delta}} C_t^{m\frac{\delta-1}{\delta}} \right]^{\frac{\delta}{1-\delta}}$$
(4)

$$C_t^d = \left[ \int C_t^d(j)^{\frac{\vartheta - 1}{\vartheta}} dj \right]^{\frac{\vartheta}{\vartheta - 1}}$$
(5)

$$C_t^m = \left[ \int C_t^m(j)^{\frac{\vartheta-1}{\vartheta}} dj \right]^{\frac{\vartheta}{\vartheta-1}}$$
(6)

The domestic price index (CPI) that is consistent with the specification of the utility function is then given by

$$P_t = \left[ (1 - \alpha) P_t^{d1 - \delta} + \alpha P_t^{m1 - \delta} \right]^{\frac{1}{1 - \delta}}$$
(7)

This specification implies that in steady state, domestichouseholds spend a fraction  $(1 - \alpha)$  of their income on domestically produced goods.

#### 2.3 Import Demand

The domestic demand for imported goods  $C_t^m$  can be shown to be

$$C_t^m = C_t \exp(v_t^m) (\exp \tau_t)^{-\delta}$$
(8)

which depends on the relative price of imports  $\tau_t$  as perceived by the domestic consumer

$$\tau_t = \log\left(\frac{P_t^m}{P_t}\right) \tag{9}$$

Thus, the cheaper are imported goods relative to domestic goods, the larger will be the share of imported goods in the consumption bundle. The exogenous shock  $v_t^m$  to the domestic consumers' demand for imported goods is assumed to follow an AR(1) process

$$v^m = \rho_m v_{t-1}^m + \varepsilon_t^m \tag{10}$$

$$\boldsymbol{\varepsilon}_t^m \sim N(0, \boldsymbol{\sigma}_m^2)$$
 (11)

The exogenous shock is needed to match the data, but ideally should only explain a small portion of the dynamics of imports.

### 2.4 The Domestic Budget Constraint and International Financial Flows

The representative household optimises the utility function (1) subject to its flow budget constraint

$$B_{t+1} + B_{t+1}^* + C_t - \frac{\psi}{2} B_t^{*2} = Y_t + (\exp v_t^{px} - 1) X_t + R_t \frac{P_{t-1}}{P_t} B_t + \frac{S_t P_{t-1} R_t^* B_t^*}{S_{t-1} P_t}$$
(12)

The variables on the left-hand side are expenditure items and the terms on the right-hand side are income items.  $B_t(i)$  and  $B_t^*(i)$  are domestic and foreign bonds, respectively, where both are expressed in real domestic terms. Their respective nominal returns are  $R_t$  and  $R_t^*$ .  $S_t$  is the nominal exchange rate defined such that an increase in  $S_t$  implies a depreciation of the domestic currency. The term  $\frac{\Psi}{2}B_t^{*2}$  is a cost paid by domestic households when they are net borrowers in the aggregate.<sup>4</sup> This ensures that the net asset position of the domestic economy is stationary and it implies that, *ceteris paribus*, a highly indebted country will have a higher equilibrium interest rate.  $Y_t$  on the right-hand side is real GDP and the term (exp  $v_t^{px}$ ) $X_t$  is export income adjusted for exogenous fluctuations in the price of exports (more on this below).

Assuming a zero net supply of domestic bonds we can write the flow budget constraint as a difference equation describing the evolution of the net foreign asset position

$$B_{t+1}^* = \frac{S_t P_{t-1} R_t^* B_t^*}{S_{t-1} P_t} + \frac{\psi}{2} B_t^{*2} + \left(\exp v_t^{px}\right) X_t - C_t^m$$
(13)

where the change in the net foreign asset position is the difference between income received for exports and expenditure on imports plus valuation effects

<sup>&</sup>lt;sup>4</sup> See Benigno (2001).

from inflation and changes in the nominal exchange rate and the net debtor cost  $\frac{\Psi}{2}B_t^{*2}$ . Households choose consumption subject to the flow budget constraint given by Equation (12). Optimally allocating consumption over time yields the standard consumption Euler equation

$$U_{c}(C_{t}) = \beta E_{t} R_{t} \frac{P_{t} U_{c}(C_{t+1})}{P_{t+1}}$$
(14)

where  $U_c(C_t)$  is the marginal utility of consumption in period *t*. Households also choose between allocating their savings to bonds denominated in the domestic and foreign currency. Equating the marginal expected return on foreign and domestic bonds yields the uncovered interest rate parity (UIP) equilibrium condition

$$R_t = \left(\exp v_t^s\right) E_t \frac{R_t^*}{\psi B_t^*} \frac{S_t}{S_{t+1}}$$
(15)

where  $v_t^s$  is a time-varying 'risk premium' that is assumed to follow the AR(1) process

$$v_t^s = \rho_s v_{t-1}^s + \varepsilon_t^s \tag{16}$$

$$\varepsilon_t^s \sim N\left(0, \sigma_s^2\right)$$
 (17)

The time-varying and persistent risk premium  $v_t^s$  is usually necessary to account for the observed deviations of the exchange rate from that implied by the UIP condition. There is no consensus in the literature on the causes of the deviations and the interpretation of the risk premium shock does not have to be literal.<sup>5</sup>

#### 2.5 Firms

The domestic economy is populated by two types of firms: producers and importers. Domestic producers indexed by j use labour as the sole input to manufacture differentiated goods with a linear technology

$$Y_t(j) = \exp(a_t) N_t(j) \tag{18}$$

<sup>&</sup>lt;sup>5</sup> See, for instance, Bacchetta and van Wincoop (2006) for an explanation based on information imperfections.

where  $a_t$  is a sector-wide exogenous process that augments labour productivity assumed to follow

$$a_t = \rho_a a_{t-1} + \varepsilon_t^a \tag{19}$$

$$\varepsilon_t^a \sim N\left(0, \sigma_a^2\right)$$
 (20)

In addition to the production sector, there is a sector that imports differentiated goods from the world and resells them domestically.

Firms have some market power over the price of the goods that they are selling since consumers prefer a mixture of differentiated goods rather than consuming just one variety. Unlike the case when all goods are perfect substitutes, this means that consumers will not switch consumption away completely from a slightly more expensive good. In this monopolistically competitive environment firms charge a mark-up over marginal cost.

Quantities sold in a given period are demand-determined in the sense that firms are assumed to set prices in domestic currency terms and then supply the amount of goods that are demanded by consumers at that price. Both importers and domestic producers set prices according to a discrete time version of the Calvo (1983) mechanism whereby a fraction  $\theta^d$  of firms producing domestically and a fraction  $\theta^m$  of importing firms do not change prices in a given period. A fraction  $\omega$  of both the domestic producers and importers that do change prices, use a rule of thumb that links their price to lagged inflation (in their own sector). This is a two-sector generalisation of Galí and Gertler (1999) that yields two Phillips curves of the following form

$$\pi_t^d = \mu_f^d E_t \pi_{t+1}^d + \mu_b^d \pi_{t-1}^d + \lambda^d m c_t^d + v_t^\pi$$
(21)

and

$$\pi_t^m = \mu_f^m E_t \pi_{t+1}^m + \mu_b^m \pi_{t-1}^m + \lambda^m m c_t^m + v_t^\pi$$
(22)

where  $mc_t^d$  is the marginal cost of the domestic producers and  $mc_t^m$ , defined as

$$mc_t^m = \log\left(\frac{S_t P_t^*}{P_t}\right),$$
(23)

is the real unit cost at the dock of imported goods. The shock  $v_t^{\pi}$  is a cost-push shock common to both sectors. The parameters in the Phillips curves are given by

$$egin{aligned} \mu_{f}^{s} &\equiv & rac{eta heta^{s}}{m{ heta}^{s} + m{\omega} \left(1 - m{ heta}^{s} (1 - m{eta})
ight)}, \ \ \mu_{b}^{s} &\equiv & rac{m{\omega}}{m{ heta}^{s} + m{\omega} \left(1 - m{ heta}^{s} (1 - m{eta})
ight)}, \ \ m{\lambda}^{s} &\equiv & rac{\left(1 - m{\omega}
ight) \left(1 - m{ heta}^{s}
ight) \left(1 - m{ heta}^{s}m{m{eta}}
ight)}{m{ heta}^{s} + m{\omega} \left(1 - m{ heta}^{s} (1 - m{m{ heta}})
ight)}, \ \ \ s \in \{d, m\} \end{aligned}$$

and domestic CPI inflation is simply the weighted average of inflation in the two sectors

$$\pi_t = (1 - \alpha)\pi_t^d + \alpha \pi_t^m \tag{24}$$

#### 2.6 Export Demand

As mentioned above, a large share of Australian exports are commodities that are traded in markets where individual countries have little market power. The standard specification of export demand is amended to reflect the fact that Australian exports and export income depend on more than just the relative cost of production in Australia and the level of world output, as would be the case in a standard open economy model. Two shocks are added to the model. The first shock  $v_t^x$  captures variations in exports that are unrelated to the relative cost of the exported goods and the level of world output. Export volumes are then given by

$$X_t = \left(\exp v_t^x\right) \left(\frac{P_t^d}{P_t^*}\right)^{-\delta^x} Y_t^*$$
(25)

where  $Y_t^*$  is world output and  $v_t^x$  is an exogenous shock that follows the AR(1) process

$$v_t^x = \rho_x v_{t-1}^x + \varepsilon_t^x \tag{26}$$

$$\varepsilon_t^x \sim N(0, \sigma_x^2)$$
 (27)

We also want to allow for 'windfall' profits due to exogenous variations in the world market price of the commodities that Australia exports. We therefore add a shock to the export income equation, which in domestic real terms is given by

$$Y_t^x = \left(\exp v_t^{px}\right) X_t \tag{28}$$

The shock  $v_t^{px}$  is thus a shock to real income (expressed in real domestic currency terms) received for the goods that Australia exports. It is assumed to follow the AR(1) process

$$v_t^{px} = \rho_{\chi} v_{t-1}^{px} + \varepsilon_t^{px}$$
<sup>(29)</sup>

$$\varepsilon_t^{px} \sim N(0, \sigma_{px}^2)$$
 (30)

It is worth emphasising here the different implication of a shock to export *demand*,  $v_t^x$ , as opposed to a shock to export *income*,  $v_t^{px}$ : the former leads to higher export incomes and higher labour demand, while the latter improves the trade balance without any direct effects on the demand for labour by the exporting industry.

### 2.7 The World Economy

The log of world output, inflation and interest rates, denoted  $\{y_t^*, \pi_t^*, i_t^*\}$ , is assumed to follow an unrestricted vector auto regression

$$\begin{bmatrix} y_t^* \\ \pi_t^* \\ i_t^* \end{bmatrix} = M \begin{bmatrix} y_{t-1}^* \\ \pi_{t-1}^* \\ i_{t-1}^* \end{bmatrix} + \varepsilon_t^*$$
(31)

The rest of the world is assumed to be unaffected by the Australian economy, and the coefficients in *M* and the covariance matrix of the world shock vector  $\varepsilon_t^*$  can therefore be estimated separately from the rest of the model.

### 2.8 Monetary Policy

A simple way to represent monetary policy that has been found to fit central bank behaviour quite well is to let the short interest rate follow a variant of the Taylor rule, letting the interest rate be determined by a reaction function of lagged inflation, lagged output and the lagged interest rate:

$$i_{t} = \phi_{y} y_{t-1} + \phi_{\pi} \pi_{t-1} + \phi_{i} i_{t-1} + \varepsilon_{t}^{i}$$
(32)

where  $\varepsilon_t^i$  is a transitory deviation from the rule with variance  $\sigma_i^2$ . This completes the description of the structural model.<sup>6</sup>

<sup>&</sup>lt;sup>6</sup> Readers who want a detailed derivation of open economy models are referred to Corsetti and Pesenti (2005).

## **3.** Estimation Strategy

The parameters of the model are estimated using Bayesian methods that combine prior information and information that can be extracted from aggregate data series. An and Schorfheide (forthcoming) provide an overview of the methodology. Conceptually, the estimation works in the following way. Denote the vector of parameters to be estimated  $\Theta \equiv \{\gamma, \eta, \varphi, ...\}$  and the log of the prior probability of observing a given vector of parameters  $\mathscr{L}(\Theta)$ . The function  $\mathscr{L}(\Theta)$  summarises what is known about the parameters prior to estimation. The log likelihood of observing the data set Z for a given parameter vector  $\Theta$  is denoted  $\mathscr{L}(Z \mid \Theta)$ . The posterior estimate  $\widehat{\Theta}$  of the parameter vector is then found by combining the prior information with the information in the estimation sample. In practice, this is done by numerically maximising the sum of the two over  $\Theta$ , so that  $\widehat{\Theta} = \arg \max [\mathscr{L}(\Theta) + \mathscr{L}(Z \mid \Theta)].$ 

The first step of the estimation process is to specify the prior probability over the parameters  $\Theta$ . Prior information can take different forms. For instance, for some parameters, economic theory determines the sign. For other parameters we may have independent survey data, as is the case for the frequency of price changes, for example.<sup>7</sup> Priors can also be based on similar studies where data for other countries were used. The restrictions implied by the theoretical model means that prior information about a particular parameter can also be useful for identifying other parameters more sharply. For instance, it is typically difficult to separately identify the degree of price stickiness  $\theta$  and the curvature of the disutility of supplying labour  $\varphi$  just by using information from aggregate time series. However, a combination of the two variables may have strong implications for the likelihood function (that is, there may be a 'ridge' in the likelihood surface). Survey evidence suggests that the average frequency of price changes is somewhere between 5 and 13 months. By choosing a prior probability for the range of the stickiness parameter  $\theta$  that reflects this information, we may also identify  $\varphi$  more sharply.

Unfortunately, we do not have independent information about all of the parameters of the model. A cautious strategy when hard priors are difficult to find is to use diffuse priors, that is, to use prior distributions with wide dispersions. If the data are informative, the dispersion of the posterior should be smaller than that of the

<sup>&</sup>lt;sup>7</sup> See Bils and Klenow (2004) and Alvarez *et al* (2005).

prior. However, Fukac *et al* (2006) point out that using informative priors, even with wide dispersions, can affect the posteriors in non-obvious ways.

Arguably, hard prior information exists for the discount factor  $\beta$ , the steady state share of imports/exports in GDP  $\alpha$  and the average duration of good prices  $\theta^d$  and  $\theta^m$ . The first two can be deduced from the average real interest rate and the average share of imports and exports of GDP and are calibrated as  $\{\beta, \alpha\} = \{0.99, 0.18\}$ . Calibration can be viewed as a very tight prior. The price stickiness parameters  $\theta^d$  and  $\theta^m$  are assigned priors that are centered around the mean duration found in European data (see Alvarez *et al* 2005).

The prior distributions of the variances of the exogenous shocks are truncated uniform over the interval  $[0,\infty)$ . It is common to use more restrictive priors for the exogenous shocks, as for example in Smets and Wouters (2003), Lubik and Schorfheide (forthcoming), Justiniano and Preston (2005) and Kam, Lees and Liu (2006), but since most shocks are defined by the particular model used, it is unclear what the source of the prior information would be.

The priors of the variances of the measurement error parameters are uniform distributions on the interval  $[0, \sigma_{Zn}^2)$  where  $\sigma_{Zn}^2$  is the variance of the corresponding time series. Economic theory dictates the domains of the rest of the priors, but we have little information about their modes and dispersions. These priors are therefore assigned wide dispersions. Information about the prior distributions for the individual parameters are given in Table 1.

### **3.1** Mapping the Model into Observable Time Series

The model of Section 2 is solved by first taking linear approximations of the structural equations around the steady state and then finding the rational expectations equilibrium law of motion. The linearised equations are listed in the Appendix and the Söderlind (1999) algorithm was used to solve the model. The solution can be written in VAR(1) form

$$X_t = AX_{t-1} + C\varepsilon_t. \tag{33}$$

where  $X_t$  is a vector containing the variables of the model, and the coefficient matrices *A* and *C* are functions of the structural parameters  $\Theta$ . Equation (33) is called the *transition equation*. The next step is to decide which (combinations) of

Table 1: Prior and Posterior Distributions of Parameters								
Parameter	Distribution	Prior		Posterior				
	-	Mode	Standard error	Mode	Standard error			
Households and firms								
γ	normal	3	0.44	3.37	0.36			
η	normal	2	0.66	1.20	0.15			
φ	normal	2	0.44	1.89	0.43			
ω	beta	0.3	0.10	0.73	0.06			
δ	normal	1	0.10	0.93	0.10			
$\delta^x$	normal	1	0.10	0.02	0.01			
θ	beta	0.75	0.04	0.73	0.04			
$\theta^m$	beta	0.75	0.04	0.90	0.02			
ψ	normal	0.01	0.02	0.10	0.02			
Taylor rule								
$\phi_{v}$	normal	0.5	0.25	0.02	0.01			
$\phi_{\pi}$	normal	1.5	0.29	0.19	0.04			
$\phi_i$	beta	0.5	0.25	0.87	0.03			
		Exogeno	us persistence					
$ ho_a$	beta	0.5	0.28	0.65	0.07			
$ ho_s$	beta	0.5	0.28	0.07	0.01			
$ ho_{px}$	beta	0.5	0.28	0.87	0.06			
$\rho_x$	beta	0.5	0.28	0.89	0.06			
$ ho_m$	beta	0.5	0.28	0.71	0.13			
Exogenous shock variances								
$\sigma_a^2$	uniform	[0,∞)		$4.66 \times 10^{-5}$	$1.59 \times 10^{-5}$			
$\sigma_v^2$	uniform	[0,∞)		$4.65 \times 10^{-2}$	$5.68 \times 10^{-3}$			
$\sigma_c^2$	uniform	[0,∞)		$2.32 \times 10^{-5}$	$7.03 \times 10^{-6}$			
$\sigma_{\pi}^2$	uniform	[0,∞)		$6.79 \times 10^{-6}$	$2.47 \times 10^{-6}$			
$\sigma_{px}^2$	uniform	[0,∞)		$5.32 \times 10^{-5}$	$1.74 \times 10^{-5}$			
$\sigma_x^2$	uniform	[0,∞)		$7.63 \times 10^{-4}$	$6.38 \times 10^{-4}$			
$\sigma_m^2$	uniform	[0,∞)		$1.34 \times 10^{-5}$	$4.44 \times 10^{-6}$			
$\sigma_i^2$	uniform	[0,∞)		$7.20 \times 10^{-7}$	$1.85 \times 10^{-7}$			

the variables in  $X_t$  are observable. The mapping from the transition equation to observable time series is determined by the *measurement equation* 

$$Z_t = DX_t + \mathbf{e}_t \tag{34}$$

The selector matrix D maps the theoretical variables in the state vector  $X_t$  into a vector of observable variables  $Z_t$ . The term  $\mathbf{e}_t$  is a vector of measurement errors. For theoretical variables that have clear counterparts in observable time series, the measurement errors capture noise in the data-collecting process. The measurement errors may also capture discrepancies between the theoretical concepts of the model and observable time series. For instance, GDP, non-farm GDP and market sector GDP all measure output, but none of these measures correspond exactly to the model's variable  $Y_t$ . The measure of total GDP includes farm output, which varies due to factors other than technology and labour inputs, most notably the weather. One may therefore want to exclude farm products. But in the model, more abundant farm goods will lead to higher overall consumption and lower marginal utility, and perhaps also higher exports, so excluding it altogether is also not appropriate. Total GDP also includes government expenditure which is not determined by the utility maximising agents of the model, but it will affect the aggregate demand for labour and therefore market wages. The state space system, that is, the transition Equation (33) and the measurement Equation (34), is quite flexible and can incorporate all three measures of GDP, allowing the data to determine how well each of them corresponds to the model's concept of output. This multiple indicator approach was proposed by Boivin and Giannoni (2005) who argue that not only does this allow us to be agnostic about which data to use, but by using a larger information set it may also improve estimation precision.

Some, but not all, of the observable time series are assumed to contain measurement errors, and the magnitude of these are estimated together with the rest of the parameters. Counting both measurement errors and the exogenous shocks, the total number of shocks in the model are more than is necessary to avoid stochastic singularity. That is, the total number of shocks are larger than the total number of observable variables in  $Z_t$ . It is reasonable to ask whether all of the shocks can be identified, and the answer is that it depends on the actual datagenerating process. The measurement errors are white noise processes specific to the relevant time series that are uncorrelated with other indicators as well as with their own leads and lags. To the extent that the cross-equation and dynamic

implications that distinguish the structural shocks from the measurement errors of the model are also present as observable correlations in the time series, it will be possible to identify the structural shocks and the measurement errors separately. Incorrectly excluding the possibility of measurement errors may bias the estimates of the parameters governing both the persistence and variances of the structural shocks. Also, by estimating the magnitude of the measurement errors we can get an idea of how well different data series match the corresponding model concept.

#### 3.2 Computing the Likelihood

The linearised model (33) and the measurement Equation (34) can be used to compute the covariance matrix of the theoretical one-step-ahead forecast errors implied by a given parameterisation of the model. That is, without looking at any data, we can compute what the covariance of our errors would be if the model was the true data-generating process and we used the model to forecast the observable variables. This measure, denoted  $\Omega$ , is a function of both the assumed functional forms and the parameters and is given by

$$\Omega = DPD' + E\mathbf{e}_t \mathbf{e}_t' \tag{35}$$

where P is the covariance matrix of the one-period-ahead forecast errors of the state

$$P = A(P - PD'(DPD' + E\mathbf{e}_t\mathbf{e}_t')^{-1}DP)A' + CE\varepsilon_t\varepsilon_t'C'$$
(36)

The covariance of the theoretical forecast errors  $\Omega$  is used to evaluate the likelihood of observing the time series in the sample, given a particular parameterisation of the model. Formally, the log likelihood of observing Z given the parameter vector  $\Theta$  is

$$\mathscr{L}(Z \mid \Theta) = -.5 \sum_{t=0}^{T} \left[ p \ln(2\pi) + \ln |\Omega| + u_t' \Omega^{-1} u_t \right]$$
(37)

where  $p \times T$  are the dimensions of the observable time series Z and  $u_t$  is a vector of the actual one-step-ahead forecast errors from predicting the variables in the sample Z using the model parameterised by  $\theta$ . The actual (sample) one-step-ahead forecast errors can be computed from the innovation representation

$$\widehat{X}_{t+1} = A\widehat{X}_t + Ku_t \tag{38}$$

$$u_t = Z_t - D\hat{X}_t \tag{39}$$

where *K* is the Kalman gain

$$K = PD'(DPD' + E\mathbf{e}_t\mathbf{e}_t')^{-1}$$

The method is described in detail in Hansen and Sargent (2005).

To help understand the log likelihood function intuitively, consider the case of only one observable variable so that both  $\Omega$  and  $u_t$  are scalars. The last term in the log likelihood function (37) can then be written as  $u_t^2/\Omega$ , so for a given squared error  $u_t^2$  the log likelihood increases in the variance of the model's forecast error variance. This term will thus make us choose parameters in  $\theta$  that make the forecast errors of the model large since a given error is more likely to have come from a parameterisation that predicts large forecast errors. The determinant term  $\ln |\Omega|$  (the determinant of a scalar is simply the scalar itself) counters this effect, and to maximise the complete likelihood function we need to find the parameter vector  $\Theta$  that yields the optimal trade-off between choosing a model that can explain our actual forecast errors,  $u_t$ , while not making the implied theoretical forecast errors too large.

Another way to understand the likelihood function is to recognise that there are (roughly speaking) two sources contributing to the forecast errors  $u_t$ , namely shocks and incorrect parameters. The set of parameters  $\Theta$  that maximise the log likelihood function (37) are those that reduce the forecast errors caused by incorrect parameters as much as possible by matching the theoretical forecast error variance  $\Omega$  with the sample forecast error covariance  $Eu_tu'_t$ , thereby attributing all remaining forecast errors to shocks.

### 3.3 The Data

The data sample is from 1991:Q1 to 2006:Q2 where the first eight observations are used as a convergence sample for the Kalman filter. Thirteen time series were used as indicators for the theoretical variables of the model, which is more than that of most other studies estimating structural small open economy models. Lubik and Schorfheide (forthcoming) estimate a small open economy model on data for Canada, the UK, New Zealand and Australia using terms of trade as the only observable variable relating to the open economy dimension of the model. Similarly, in Justiniano and Preston (2005) the real exchange rate between the US and Canada is the only data series relating to the open economy dimension of the

model. Neither of these studies use trade volumes to estimate their models. This is also true for Kam *et al* (2006), though this study uses data on imported goods prices rather than only aggregate CPI inflation.

In this paper, data for the rest of the world are based on trade-weighted G7 output and inflation and an (unweighted) average of US, Japanese and German/euro interest rates. Three domestic indicators that are assumed to correspond exactly to their respective model concepts are the cash rate, the nominal exchange rate, and trimmed mean quarterly CPI inflation. The rest of the domestic indicators are assumed to contain measurement errors. These are GDP, non-farm GDP, market sector GDP, exports as a share of GDP, the terms of trade (defined as the price of exports over the price of imports) and labour productivity. All real variables are linearly detrended and inflation and interest rates were demeaned. The correspondence between the data series and the model concepts are described in Table 2.

Table 2: Indicators and Estimated Measurement Errors					
Data	Model	$\Sigma_{ee}/\Sigma_{_{ZZ}}$			
Interest rate	$i_t$	_			
Nominal exchange rate change	$\Delta s_t$	—			
CPI trimmed mean inflation	$\pi_t$	—			
Real GDP	$y_t$	0.03			
Real non-farm GDP	$y_t$	0.05			
Real market sector GDP	$y_t$	0.15			
Export share of GDP	$x_t - y_t$	0.02			
Import share of GDP	$c_t^m - y_t$	0.00			
Terms of trade	$v_t^{px} - mc_t^m$	0.84			
Labour productivity	$a_t$	0.11			

# 4. Estimation Results

Table 1 reports the mode and standard deviation of the prior and posterior distributions of the structural parameters of the model. The posterior modes were found using Bill Goffe's simulated annealing algorithm. The posterior distribution was generated by the Random-Walk Metropolis Hastings algorithm using 1.5 million draws, where the starting value for the parameter vector is the mode of the posterior as estimated by the simulated annealing algorithm. Ideally, the posterior distributions should have a smaller variance than the prior distribution

since this would indicate that the data are informative about the parameters. For most of the parameters this is the case. Two exceptions are the labour supply elasticity  $\varphi$  and the price elasticity of consumption of imported goods,  $\delta$ . This suggests that the values of these parameters do not have strong implications for the dynamics of the observable time series.

The fraction of price setters whose behaviour follows a rule of thumb is estimated to be 0.73, a larger fraction than usual; see, for example, Smets and Wouters (2003), Lubik and Schorfheide (forthcoming), and Justiniano and Preston (2005). This parameter may also capture other sources of inflation inertia, for instance from information imperfections as in Mankiw and Reis (2002) and Woodford (2001). Imports seem to be more price elastic than exports, as evidenced by the significantly larger estimated value of  $\delta$  as compared to  $\delta^x$ . The estimated frequency of price changes in the imported goods sector is lower than that estimated for prices in the domestically produced goods sector.

The parameters in the Taylor rule suggest that policy responses to inflation and output are very gradual, with a high estimated value for the parameter on the lagged interest rate. The response of the short interest rate to output deviations is quite small, with the short interest rate appearing to respond mostly to inflation.

### 4.1 Model Fit

The in-sample fit of the model can be assessed by plotting the one-period-ahead forecasts against the actual observed indicators (Figure 1).

The model provides a very good in-sample description of the dynamics of the cash rate, which is likely to be primarily because its persistence makes it easy to predict. The model is also able to fit most of the other time series reasonably well, with the exception of the terms of trade.

The variances of the errors in the measurement Equation (34) are estimated jointly with the structural parameters of the model. These variances capture series-specific transitory shocks to the observable time series. A low estimated measurement error variance indicates that the associated observable time series matches the corresponding model concept closely. The ratios of the measurement errors over the variance of the corresponding time series are reported in Table 2.



Figure 1: Actual and Model's One-period-ahead Forecasts

The variance ratios for the various measures of GDP are particularly interesting, since we used multiple indicators for this variable. The estimated values of these ratios indicate that real GDP appears to conform slightly better to the dynamicand cross-equation implications of the model than real non-farm GDP, but the difference is small. The third indicator for output – domestic market sector GDP – appears to provide the poorest fit.

The terms of trade again stands out as the time series that the model has the biggest problem fitting; the variance of the terms of trade is estimated to be almost entirely due to measurement errors.

### 4.2 The Open Economy Dimension of the Model

Table 3 below reports the variance decomposition<sup>8</sup> of the model evaluated at the estimated posterior modes reported in Table 1. The first row contains the fraction of the variances that originate from outside Australia. Foreign shocks explain 65 per cent, 67 per cent and 58 per cent respectively of the variance of domestic output, inflation and interest rates. If, instead, a reduced-form VAR(4) in world and domestic output, inflation and interest rates is estimated (with the world variables assumed to be exogenous to the domestic variables), the results suggest that foreign shocks are responsible for 49 per cent, 32 per cent and 45 per cent of the domestic variance of output, inflation and interest rates rates rates rates respectively. The structural model parameterised at the posterior mode thus attributes *more* of the variance of domestic variables to foreign shocks than the reduced-form regressions; although for output and inflation, the 95 per cent probability intervals include the estimates from the VAR(4).

The fact that the model can match the reduced-form evidence of the influence of foreign shocks on the Australian economy is reassuring, but is at odds with some previous studies. Justiniano and Preston (2005), using Canadian and US data, find that reduced-form estimates imply that a sizable fraction of domestic volatility does indeed originate abroad. However, their structural model attributes less than 1 per cent to foreign sources. They interpret this as a failure of their structural model to capture the open economy aspects of the data, in spite of its ability to replicate the cross-correlations and dynamics of the Canadian variables.

Apart from the fact that the models are estimated using data for different countries, what can explain this difference in results? One reason may be that Justiano and Preston let the US proxy for the world economy while in this paper the rest of the world is represented by trade-weighted data on a larger set of countries. Any shock that emanates from outside the US, for instance, from Europe, will be attributed

<sup>&</sup>lt;sup>8</sup> The variance decomposition is for the model variables, not the observable time series. For time series that are estimated to contain only a small measurement error component, the numbers in Table 3 are also a relatively accurate approximation to the variance decomposition of the observed times series.

Table 3: Variance Decomposition						
Shock/variable		Output	Inflation	Exports	$\Delta$ Exchange	Interest
					rate	rate
		У	$\pi$	x	$\Delta s$	i
Foreign	$\varepsilon_t^*$	0.65	0.67	0.97	0.88	0.58
		(0.44–0.80)	(0.38–78)	(0.85–1)	(0.76–0.95)	(0.46–0.91)
Productivity	$\boldsymbol{\varepsilon}^{a}$	0.01	0.01	0	0	0
		(0-0.16)	(0-0.11)	(0–0)	(0-0.01)	(0-0.01)
UIP risk	$\boldsymbol{\varepsilon}^{v}$	0	0	0	0.01	0.01
premium		(0–0)	(0–0)	(0–0)	(0.01–0.01)	(0–0)
Demand	$\boldsymbol{\varepsilon}^{\boldsymbol{y}}$	0.04	0	0	0	0
		(0.01–0.19)	(0-0.01)	(0–0)	(0–0)	(0-0.01)
Cost push	$\varepsilon^{\pi}$	0.06	0.07	0	0	0.04
		(0.02–0.15)	(0.04–0.22)	(0–0)	(0–0)	(0.02–0.10)
Export price	$\boldsymbol{\varepsilon}^{px}$	0.01	0.01	0	0.01	0
		(0.01–0.05)	(0-0.04)	(0-0.01)	(0-0.01)	(0-0.03)
Export	$\boldsymbol{\varepsilon}^{x}$	0.21	0.23	0.03	0.10	0.24
demand		(0.07–0.33)	(0.12–0.42)	(0.02–0.14)	(0.07–0.16)	(0.11–0.43)
Import	$\varepsilon^m$	0	0	0	0	0
demand		(0–0)	(0–0)	(0–0)	(0–0)	(0–0)
Taylor rule	$\varepsilon^{i}$	0.01	0.01	0	0	0.02
		(0-0.04)	(0-0.03)	(0–0)	(0–0)	(0.01–0.07)
Note: Figures in brackets indicate 95 per cent posterior probability intervals.						

to the US in their reduced-form exercise, but it is not clear that a European shock will be appropriately captured by the bilateral US-Canada data.

Another reason why the present model may better capture the impact of foreign shocks is that it is estimated using data on trade volumes. Not using data on imports and exports makes it harder for any model to distinguish between domestic demand shocks and demand for the domestically produced goods coming from abroad.

Table 3 also shows that the model can explain almost all of the nominal exchange rate variance endogenously. The exogenous UIP risk premium shock accounts for

only about 1 per cent of the variance of the nominal exchange rate and there is thus less of an exchange rate disconnect puzzle than is found by most other studies.<sup>9</sup>

These results are not significantly affected by the inclusion of measurement errors in some of the time series. Re-estimating the model without measurement errors does increase the posterior mode estimate of the variance of the nominal exchange rate attributable to risk premium shocks, but only to 4 per cent, which is still a much lower figure than that of other studies. Also, the fraction of output variance attributable to foreign shocks falls to 55 per cent and the variance of the interest rate attributable to foreign sources falls to 36 per cent and is thus closer to the reduced-form evidence than the estimated values when measurement errors are included. The fraction of domestic inflation variance attributable to foreign sources for the interest increases to over 80 per cent without measurement errors.<sup>10</sup>

The importance of exogenous export demand and income shocks for the dynamics of the model can also be gauged from Table 3. The exogenous export demand shock appears to be more important for explaining output, inflation, the exchange rate and the interest rate than for explaining the variance of exports, which may seem odd at first glance. A possible explanation for this could be that when increased export demand is driven by world developments (which dominates the variance decomposition for exports), imports increase and production for domestic consumption falls. The exogenous demand shock could then be the component of export demand that is not associated with a similar switch of production away from domestic consumption goods. This would lead to the exogenous export demand shock being important for the variance of domestic output, but not very important for the overall variance of exports.

<sup>&</sup>lt;sup>9</sup> The literature on the exchange rate disconnect puzzle is very large. The seminal paper that defined the 'puzzle' is Meese and Rogoff (1983), who showed that exchange rates are very volatile and appear to be disconnected from the macro fundamentals. Examples of recent papers that find a much larger role for the UIP shock are Lubik and Schorfheide (2005) and Lindé *et al* (2004).

<sup>&</sup>lt;sup>10</sup> The model without measurement errors was estimated using real GDP as the only indicator for domestic output. More details of the model estimates without measurement errors are available from the author upon request.

### 4.3 The Impact of a Monetary Policy Shock

Figure 2 below displays the impulse responses to a unit shock to the (annualised) cash rate for selected endogenous variables together with the 95 per cent highest marginal likelihood intervals.



An unanticipated increase in interest rates leads to a fall in output with the maximum negative response of 1.3 percentage points occurring after three quarters. There are two factors contributing to the fall in output. First, the higher real interest rate leads to a fall in domestic consumption. Second, the higher return on domestic bonds leads to a higher demand for the domestic currency denominated assets, leading to a currency appreciation. Lower domestic

consumption and less demand for labour both reduce the market real wage, causing a fall in inflation. This is reinforced by the appreciating exchange rate which makes imports cheaper and further decreases inflation. (However, initially consumer prices of imported goods do not fall as much as domestically produced goods, which makes imported goods initially relatively more expensive.) The peak response of (annualised) inflation to the unit shock to the interest rate is a fall of approximately 0.4 percentage points three quarters after impact. The estimated maximum response of output and inflation to a monetary policy shock is faster than that which is found in some other studies, including those employing SVARs.<sup>11</sup> Some of this difference may be explained by the relatively stringent restrictions imposed by the structural model compared to an SVAR. Another factor that could contribute to the relatively rapid response to a monetary policy shock in the present model may be that the sample used does not include the change to an inflation-targeting regime in the early 1990s. If the credibility of the new monetary policy regime was established only gradually, then this could contribute to relatively slow estimated responses of inflation and output to an increase in the cash rate for studies that incorporate this transitory period.

### 4.4 The Impact of Export Demand and Income Shocks

The effects of an exogenous increase in the demand for Australian exports are illustrated in Figure 3. A 1 percentage point increase in export demand leads on impact to a 0.2 percentage point increase in GDP (consistent with the share of the export sector in GDP). It also leads to an appreciation of the exchange rate and boosts imports. The appreciating exchange rate leads to a fall in inflation, though it is quantitatively small (less than 0.03 percentage points at the maximum impact). These effects can be contrasted with the estimated response to a positive shock to the export price. Remember, the main difference between the export price and demand shock is that a price shock does not put direct pressure on the domestic labour market. Figure 4 shows that an income shock, like a demand shock, leads to an appreciation of the exchange rate. The response of the endogenous variables are very similar, with the exception of the volume of exports, which falls due to the appreciating exchange rate. Due to the low elasticity of export demand, the quantitative effect is small.

<sup>&</sup>lt;sup>11</sup> See for instance Dungey and Pagan (2000) and Berkelmans (2005).





### 4.5 The Impact of a Productivity Shock

Figure 5 plots the impulse responses to a unit shock to Australian productivity. As expected, GDP increases, inflation falls and the nominal exchange rate appreciates. A less obvious effect is that the consumption of imported goods falls in spite of the appreciating exchange rate. This is because domestic goods prices fall sufficiently so as to make imports relatively more expensive.



**Figure 5: Productivity Shock** 

# 5. Conclusion

This paper presents a small structural model of the Australian economy estimated using Bayesian techniques and based on a standard New Keynesian small open economy specification similar to that used by numerous other studies. However, there are four aspects in which the estimation of the model deviates from previous studies.

The first is that the export demand and export income equations are amended with exogenous shocks to control for the prominent role played by commodities in the Australian export sector. When the model is estimated, the export demand shock appears to play a larger role than the export income shock in explaining the variance of domestic variables.

Second, a larger number of time series were used to estimate the model. In particular, data on import and export volumes were used in addition to the standard aggregate variables to ensure that the data span the open economy dimension of the model.

Third, flat prior distributions were used for the variances of the structural shocks. This reflects the fact that most of the structural shocks are defined jointly by the model and the data with little or no role for economic theory nor independent sources of information to help determine the magnitude of these shocks.

Fourth, the magnitude of measurement errors in some of the time series were estimated together with the structural parameters of the model. This acknowledges the fact that not only is error sometimes introduced through the data collection process, but also that the model variables do not always have clear-cut counterparts in observable time series.

The estimated model provides a good fit for most of the observable variables and appears to be able to capture the open economy dimensions of the data reasonably well. The model can match the evidence from reduced-form studies on the importance of foreign shocks to the domestic variance of output, inflation and interest rates. The model also relies much less than other estimated structural models on a persistent UIP risk premium shock to explain movements in the nominal exchange rate. Given the simplicity of the model, these results hold promise for the usefulness of these types of open economy models as analytical tools. However, there are other dimensions in which the model performs less well. Particularly, movements in the terms of trade are not well captured by the model and the reasons for this should be a subject of future investigation.

# **Appendix A: The Linearised Model**

The consumption Euler Equation

$$c_{t} = \frac{\gamma}{\gamma - \eta + \gamma \eta} E_{t} c_{t+1} + \frac{-\eta (1 - \gamma)}{\gamma - \eta + \gamma \eta} c_{t-1} - \frac{1}{\gamma - \eta + \gamma \eta} \left( i_{t} - E_{t} \pi_{t+1} \right) + v_{t}^{d} \quad (A1)$$

Import demand

$$c_t^m = c_t - \delta \tau_t + v_t^m \tag{A2}$$

Domestic consumption demand

$$c_t^d = c_t + \delta \tau_t \tag{A3}$$

The relative price of imported goods for the domestic consumer

$$\tau_t = \tau_{t-1} + \pi_t^m - \pi_t \tag{A4}$$

Export demand

$$x_t = -\delta^x \tau_t^* + Y_t^* + v_t^x \tag{A5}$$

The relative price of goods produced domestically sold to the world

$$\tau_t^* = \pi_t - \pi_t^* - \Delta s_t + \tau_{t-1}^*$$
 (A6)

Domestic production (resource constraint)

$$y_t = (1 - \alpha)c_t^d + \alpha x_t \tag{A7}$$

Inflation of domestically produced goods

$$\pi_t^d = \mu_f^d E_t \pi_{t+1}^d + \mu_b^d \pi_{t-1}^d + \lambda m c_t^d$$
(A8)

Inflation of imported goods

$$\pi_t^m = \mu_f^m E_t \pi_{t+1}^m + \mu_b^m \pi_{t-1}^m + \lambda m c_t^m$$
(A9)

**CPI** inflation

$$\pi_t = (1 - \alpha) \, \pi_t^d + \alpha \pi_t^m \tag{A10}$$

Uncovered interest rate parity condition

$$i_t - i_t^* = \Delta E_t s_{t+1} - \psi b_t^* + v_t^s$$
 (A11)

Flow budget constraint

$$b_{t+1}^* = b_t^* + x_t - c_t^m + v_t^{px} + \Delta s_t$$
(A12)

Labour supply decision

$$w_t - p_t - \gamma \left( c_t - \eta c_{t-1} \right) = \varphi n_t \tag{A13}$$

$$w_t - p_t = \varphi(y_t - a_t) + \gamma(c_t - \eta c_{t-1})$$
 (A14)

Real domestic marginal cost (the real wage divided by marginal productivity of labour)

$$mc_t = \gamma \left( c_t - \eta c_{t-1} \right) + \varphi n_t - a_t \tag{A15}$$

or

$$mc_t = \gamma c_t - \gamma \eta c_{t-1} + \varphi y_t - (\varphi + 1)a_t$$
(A16)

Real marginal cost of imported goods

$$mc_t^m = s_t + p_t^w - p_t \tag{A17}$$

or

$$mc_t^m = \Delta s_t + \pi_t^w - \pi_t + mc_{t-1}^m \tag{A18}$$

The Taylor rule describing monetary policy

$$i_t = \phi_y y_{t-1} + \phi_\pi \pi_{t-1} + \phi_i i_{t-1} + \varepsilon_t^i$$
 (A19)

### References

Álvarez LJ, E Dhyne, MM Hoeberichts, C Kwapil, H Le Bihan, P Lünneman, F Martins, R Sabbatini, H Stahl, P Vermeulen and J Vilmunen (2005), 'Sticky Prices in the Euro Area: A Summary of New Micro Evidence', European Central Bank Working Paper Series No 563.

An S and F Schorfheide (forthcoming), 'Bayesian Analysis of DSGE Models', *Econometric Review*.

**Bacchetta P and E van Wincoop (2006),** 'Can Information Heterogeneity Explain the Exchange Rate Determination Puzzle?', *American Economic Review*, 96(3), pp 552–576.

**Benigno P** (2001), 'Price Stability with Imperfect Financial Integration', Centre for Economic Policy Research Working Paper No 2854.

**Berkelmans L** (2005), 'Credit and Monetary Policy: An Australian SVAR', Reserve Bank of Australia Research Discussion Paper No 2005-06.

**Bils M and PJ Klenow (2004),** 'Some Evidence on the Importance of Sticky Prices', *Journal of Political Economy*, 112(5), pp 947–985.

**Boivin J and M Giannoni (2005), 'DSGE Models in a Data-Rich Environment',** Columbia University, unpublished manuscript.

**Calvo GA (1983),** 'Staggered Prices in a Utility-Maximizing Framework', *Journal of Monetary Economics*, 12(3), pp 383–398.

**Corsetti G and P Pesenti (2005),** 'The Simple Geometry of Transmission and Stabilization in Closed and Open Economies', NBER Working Paper No 11341.

**Department of Foreign Affairs and Trade (2005),** *Composition of Trade*, available at <a href="http://www.dfat.gov.au/publications/>">http://www.dfat.gov.au/publications/</a>.

**Dungey M and A Pagan (2000),** 'A Structural VAR Model of the Australian Economy', *The Economic Record*, 76(235), pp 321–342.

**Fukac M, A Pagan and V Pavlov (2006),** 'Econometric Issues Arising from DSGE Models', Australian National University, unpublished manuscript.

Galí J and M Gertler (1999), 'Inflation Dynamics: A Structural Econometric Analysis', *Journal of Monetary Economics*, 44(2), pp 195–222.

**Galí J and T Monacelli (2005),** 'Monetary Policy and Exchange Rate Volatility in a Small Open Economy', *Review of Economic Studies*, 72(3), pp 707–734.

Hansen L and T Sargent (2005), 'Recursive Methods for Linear Economies', University of Chicago and New York University.

**Justiniano A and B Preston (2005),** 'Can Structural Small Open Economy Models Account for the Influence of Foreign Disturbances?', Columbia University, unpublished manuscript.

Kam T, K Lees and P Liu (2006), 'Uncovering the Hit-List for Small Inflation Targeters: A Bayesian Structural Analysis', Reserve Bank of New Zealand Discussion Paper No DP2006/09.

Lindé J, M Nessén and U Söderström (2004), 'Monetary Policy in an Estimated Open-Economy Model with Imperfect Pass-Through', Sveriges Riksbank Working Paper Series No 167.

Lubik T and F Schorfheide (2005), 'A Bayesian Look at New Open Economy Macroeconomics', John Hopkins University, Department of Economics Working Paper No 521.

Lubik T and F Schorfheide (forthcoming), 'Do Central Banks Respond to Exchange Rate Movements? A Structural Investigation', *Journal of Monetary Economics*.

Mankiw G and R Reis (2002), 'Sticky Information Versus Sticky Prices: A Proposal to Replace the New Keynesian Phillips Curve', *Quarterly Journal of Economics*, 117(4), pp 1295–1328.

**Meese RA and K Rogoff (1983),** 'Empirical Exchange Rate Models of the Seventies: Do they Fit Out of Sample?', *Journal of International Economics*, 14(1–2), pp 3–24.

Nessén M (2006), 'How are DSGE Models Used in Policy-Making?', paper presented at a workshop on 'The Interface between Monetary Policy and Macro Modelling', Reserve Bank of New Zealand, Wellington, 13–15 March.

**Smets F and R Wouters (2003),** 'An Estimated Stochastic General Equilibrium Model of the Euro Area', *Journal of the European Economic Association*, 1(5), pp 1123–1175.

**Smets F and R Wouters (2004),** 'Forecasting with a Bayesian DSGE Model: An Application to the Euro Area', *Journal of Common Market Studies*, 42(4), pp 841–867.

**Söderlind P** (1999), 'Solution and Estimation of RE Macromodels with Optimal Policy', *European Economic Review*, 43(4–6), pp 813–823.

Woodford M (2001), 'Imperfect Common Knowledge and the Effects of Monetary Policy', NBER Working Paper No 8673.